

## Recent Surface Deformation along the Carmel-Gilboa Fault System, Israel

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### ABSTRACT

The Carmel-Gilboa Fault System is one of the major geological structures of northern Israel. It is a northwestern branch of the Dead Sea Fault. Tectonic activity and crustal deformation occur along the Carmel Gilboa Fault System. The fault system region is covered by a monitoring geodetic network consisting of 24 sites. In this paper we analyze GPS data which were measured eight times between 1999 and 2016 and derive regional velocities for the network sites. The site velocities were estimated with respect to a local datum. In order to define a correct datum and ensure stability of the datum we assume that GPS vectors are not immune to changes in their datum content of orientation and scale. The GPS vectors from each campaign are stripped from their datum content using the extended free network adjustment constraints. The datumless measurements are used to define the datum by preliminary coordinates and linear constraints, which remain constant for all monitoring campaigns, as well as to define the position of the network points and their velocities. The use of extended S-transformation enables transition from one datum to another and calculates the velocities in relation to the chosen datum.

We use principles from continuum mechanics to extract the horizontal site velocities field into surface deformation parameters. The results show deformations of about 1 mm/yr sinister along the Carmel Gilboa Fault System accompanied with extensions and shear strain.

### I. INTRODUCTION

Tectonic activity and crustal deformation in northern Israel occur mainly on the Dead Sea Fault (DSF) and the Carmel-Gilboa Fault System (CGFS). The DSF is a sinistral transform fault that forms the boundary between the Arabian Plate and the Sinai Sub-Plate mainly on the N-S trending (Fig 1). The CGFS is composed of several NW-SE trending faults while the main faults are the Carmel Fault (CF) and Gilboa Fault (GF) (Fig. 2). The CGFS is a branch of the DSF that starts at the Jordan Valley, goes up to the northern tip of Mount Carmel and extends into the Mediterranean Sea.

There is no agreement on the exact location of the CGFS. There are those who locate the main fault along the southwestern side of the Yizre'el Valley (for example, Hofstetter et al., 1996; Rotstein et al., 2004; Fleischer and Gafsou, 2005) and others locate the main fault somewhere within the Yizre'el Valley downfaulted structure (Segev and Rybakov, 2011). Actually, the CGFS is a wide (up to ~20 km) deformation zone on the valley's southeastern side, which narrows towards the northwest (Mount Carmel). The fault pattern within the Yizre'el Valley is not well known. Some suggested a fault system below the Yizre'el Valley, which connects the Gilboa and the Carmel faults (Segev et al., 2006; Segev et al., 2014).

Mount Carmel is an elevated and intensively faulted area that is bordered by the main Carmel Fault on the northeast. The latter is divided into two main segments:

A NW-SE oriented segment that runs from Haifa Bay towards Amaqim Junction (Jalame) and a N-S oriented fault that runs between Jalame and Yoqneam (Fig. 2). Its continuation southward is the Yoqneam Fault.

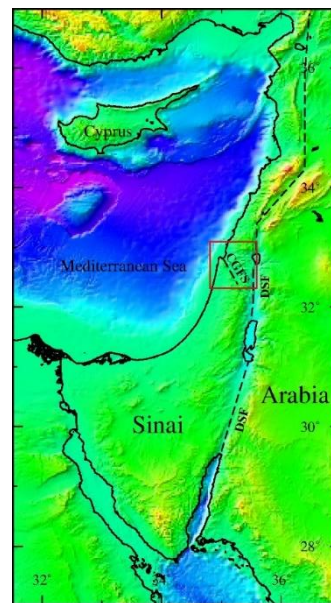


Figure 1. Tectonic map of Eastern Mediterranean showing the Sinai and Arabia plates. The black dash line denotes the location of the Dead Sea Fault (DSF). The red box denotes the study area with the Carmel Gilboa Fault System (CGFS) location.



the influence of a datum definition inherent in geodetic measurements.

The outcome of the Bernese GPS software is a minimal constrained solution of the network points and their variance-covariance matrix for each monitoring campaign, referring to a conventional terrestrial coordinate system. By applying the extended S-Transformation to the eight monitoring campaigns, we can strip the datum content of scale and orientations from the GPS vectors and estimate a velocity field free of negative effects of those factors. The extended S-Transformation was used to transform the vector of velocities ( $\dot{x}$ ) and its covariance matrix to a solution which is based on the network's datum definition, a datum which is based on a group of stable points. Congruency testing is performed to determine the stable datum points (for details see Even-Tzur and Reinking, 2013).

#### IV. DEFORMATION ANALYSIS

In two-dimensional analysis of the point velocity field we are able to compute in total six parameters of an affine transformation: the two parameters of the velocity of the network's barycenter ( $\bar{x}$   $\bar{y}$ ), the rotation parameter ( $r_z$ ) and the deformation rate tensor, which is composed of the scale factors of the two axes ( $d_{xx}^{-1}$   $d_{yy}^{-1}$ ) and the angle between them ( $d_{xy}$ ). The parameters gather in vector  $g$  as:

$$g = \left[ \bar{x} \quad \bar{y} \quad r_z \quad d_{xx}^{-1} \quad d_{yy}^{-1} \quad d_{xy} \right]^T \quad (1)$$

The scale factors present the extensions in the directions of the Cartesian coordinate axes, and the angle between them is the appropriate shearing strain.

We introduce a matrix  $B$  with the following composition:

$$B = \begin{bmatrix} 1 & 0 & -y_1 & x_1 & 0 & y_1 \\ 0 & 1 & x_1 & 0 & y_1 & x_1 \\ \cdot & \cdot & \cdot & \cdot & \cdot & \cdot \\ 0 & 1 & x_u & 0 & y_u & x_u \end{bmatrix} \quad (2)$$

The coordinates  $x_i$ , and  $y_i$  of point  $i$  ( $i=1,2,\dots,u$ ) are given in a Cartesian system that is parallel to the reference system and with an origin at the network's barycenter.

The velocity field of a group of points can be partitioned into a linear model  $B^T g$  and a residual vector  $v$ :

$$\dot{x} = Bg + v \quad (3)$$

The velocity vector  $\dot{x}$  has a cofactor matrix  $Q_x$  and the vector  $g$  and its cofactor matrix  $Q_g$  are given as:

$$\begin{aligned} g &= (B^T Q_x^{-1} B)^{-1} B^T Q_x^{-1} \dot{x} \\ Q_g &= (B^T Q_x^{-1} B)^{-1}. \end{aligned} \quad (4)$$

For a 2D network at least three non-collinear points are required to define all the elements of vector  $g$ .

It is not obligatory to estimate all the elements of vector  $g$  for a given area represented by a velocity field of some of the network points. It might be possible that only some of the parameters better describe the motion, rotation, and deformation array in a part of the area. The structure of  $B$  allows for performing a partial solution, where only part of the six possible parameters are solved with different combinations. Different sets of parameters can be assembled and tested for suitability to the area under study.

But, how can we determine what is the best set of parameters, the one which describes best the velocity field. The problem of selecting the "best" set of parameters can be solved using the Akaike's Information Criterion (AIC) (Akaike, 1974). Since in this study we deal with a small sample size, the second-order Akaike Information Criterion (AICc) is used instead AIC (Burnham and Anderson, 2002).

AICc is defined as

$$AICc = n \cdot \ln(v^T P v) + 2u / (n - u - 1) \quad (5)$$

where  $n$  is the number of observations,  $v^T P v$  is the weighted sum of squared residuals and  $u$  is the number of parameters. The AICc penalizes for the addition of parameters, and thus selects a model that fits well but has a minimum number of parameters. A good mathematical model is one that has the smallest AICc score.

#### V. RESULTS

Eight campaigns of horizontal coordinates and their variance-covariance matrices, observed over a period of 17 years, were obtained from the GPS analysis. The data was used to derive site velocities by extended free network adjustment constraints.

The estimation of velocity field was carried out by using the Two-Steps method with an adequate estimation of the variance factor (Even-Tzur, 2004). The first step is accomplished using the Bernese GPS software. The outcome of the software is a minimal constrained solution of the network points and their variance-covariance matrix for each monitoring campaign, referring to a conventional terrestrial coordinate system. By using the extended S-transformation we can strip the datum content of scale and orientations from the measured coordinates. The solution of the network points' plane position for each monitoring epoch and their variance-covariance matrix are used as pseudo-measurements for the solution of the second step, where in each solution different models can be tested to describe the plane position of the network points.

The extraction of deformation parameters from the horizontal site velocities field was done referring to the Galilee Datum. The network points in the Carmel region were tested. In total the tested area includes 15 points (see Fig. 2).

Table 1. The surface deformation parameters that compose each set and its AICc score for the Carmel tested area.

Model (c)	Deformation Parameters							AICc score
	$\bar{x}$ [mm/yr]	$\bar{y}$ [mm/yr]	$r_z$ 10 <sup>-8</sup> [rad/yr]	$d_{xx}^{-1}$ 10 <sup>-8</sup> [1/yr]	$d_{yy}^{-1}$ 10 <sup>-8</sup> [1/yr]	$d_{xy}^{-1}$ 10 <sup>-8</sup> [1/yr]	$d_{xy}$ 10 <sup>-8</sup> [rad/yr]	
1	✓	✓						149.6
2	✓	✓	✓					148.6
3	✓	✓					✓	142.9
4	✓	✓				✓		150.2
5	✓	✓	✓			✓		149.0
6	✓	✓		✓	✓			152.6
7	✓	✓	✓				✓	145.2
8	-0.63 ±0.19	0.21 ±0.16				3.7 ±0.9	4.2 ±0.6	139.2
9	✓	✓	✓	✓	✓			151.8
10	✓	✓		✓	✓		✓	142.0
11	✓	✓	✓			✓	✓	141.9
12	✓	✓	✓	✓	✓		✓	145.0

In order to define the best set of parameters, the one which describes best the velocity field, various sets of parameters were composed. The six parameters of vector  $g$  (Eq. 1) were used to create 12 sets of parameters. The deformation parameters that compose each set are presented in Table 1. The best model was determined by AICc which penalizes for the addition of parameters, and thus selects a model that fits well but has a minimum number of parameters. A good model is one that has the smallest AICc score. The AICc score of the 12 models for the Carmel tested area can be seen in Table 1 with the best set of parameters for each tested area. With a 5% level of significance, the velocity of the subnetworks' barycenter, scales and angle between the axes are significant.

## VI. DISCUSSION AND CONCLUSIONS

We use principles from continuum mechanics to extract the horizontal site velocities field into surface deformation parameters. The creation of an accurate and reliable velocity field is based on eight monitoring campaigns that were measured between 1999 and 2016, eight-hour measurement sessions, measuring each network point at least twice in each campaign and using sophisticated mathematical tools. The regional site velocities were estimated with respect to a local datum that was defined by a stable cluster of sites on one side of the fault by means of extended free net adjustment constraints and extended similarity transformation.

The use of AICc allowed us to choose the best model among several. The best model is defined as the one that better describes the velocity field.

The values of velocities and deformation parameters in the research area are very small as can be seen in

Table 1, yet the values are significant at a 95% confidence level.

In conclusion, the results show deformations of less than 1 mm/yr sinistral along the Carmel Fault accompanied by extensions and shear strain.

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